

Naive Bayes



Naive Bayes - Introduction

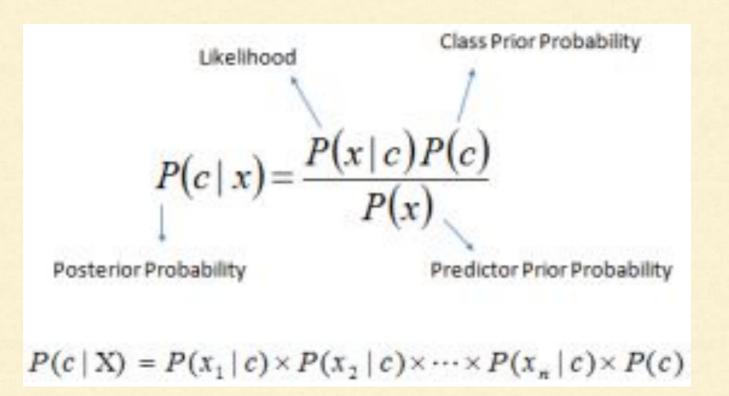
Naive Bayes - (Sometime aka Stupid Bayes :))

- Classification technique based on Bayes' Theorem
- With "naive" assumption of independence among predictors.
- Easy to build
- Particularly useful for very large data sets
- Known to outperform even highly sophisticated classification methods
 - a. e.g. Earlier method for spam detection



Introduction - Bayes theorem

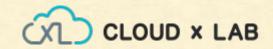
- P(c|x) the posterior probability of class (c, target) given predictor (x, attributes).
- P(c) the prior probability of class.
- P(x|c) is the likelihood which is the probability of predictor given class.
- P(x) is the prior probability of predictor.





- We are training data set of weather and corresponding target variable 'Play' (suggesting possibilities of playing).
- Now, we need to classify whether players will play or not based on weather condition.

Weather	Play
Sunny	No
Overcast	Yes
Rainy	Yes
Sunny	Yes
Sunny	Yes
Overcast	Yes
Rainy	No
Rainy	No
Sunny	Yes
Rainy	Yes
Sunny	No
Overcast	Yes
Overcast	Yes
Rainy	No



- I. Convert the data set into a frequency table
- 2. Create Likelihood table by finding the probabilities like Overcast probability = 0.29 and probability of playing is 0.64.
- 3. Now, use Naive Bayesian equation to calculate the posterior probability for each class. The class with the highest posterior probability is the outcome of prediction.

Weather	Play
Sunny	No
Overcast	Yes
Rainy	Yes
Sunny	Yes
Sunny	Yes
Overcast	Yes
Rainy	No
Rainy	No
Sunny	Yes
Rainy	Yes
Sunny	No
Overcast	Yes
Overcast	Yes
Rainy	No

Frequency Table		
Weather	No	Yes
Overcast		4
Rainy	3	2
Sunny	2	3
Grand Total	5	9

Like	elihood tab	le		
Weather	No	Yes		
Overcast		4	=4/14	0.29
Rainy	3	2	=5/14	0.36
Sunny	2	3	=5/14	0.36
All	5	9		
2.	=5/14	=9/14		
	0.36	0.64		

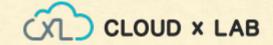


Problem: Players will play if weather is sunny. Is this statement is correct?

Weather	Play
Sunny	No
Overcast	Yes
Rainy	Yes
Sunny	Yes
Sunny	Yes
Overcast	Yes
Rainy	No
Rainy	No
Sunny	Yes
Rainy	Yes
Sunny	No
Overcast	Yes
Overcast	Yes
Rainy	No

Frequency Table		
Weather	No	Yes
Overcast		4
Rainy	3	2
Sunny	2	3
Grand Total	5	9

Like	elihood tab	le		
Weather	No	Yes		
Overcast		4	=4/14	0.29
Rainy	3	2	=5/14	0.36
Sunny	2	3	=5/14	0.36
All	5	9		
21 21	=5/14	=9/14		
	0.36	0.64		



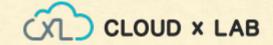
Problem: Players will play if weather is sunny. Is this statement is correct?

P(Yes | Sunny) = P(Sunny | Yes) * P(Yes) / P (Sunny)

Weather	Play	
Sunny	No	
Overcast	Yes	
Rainy	Yes	
Sunny	Yes	
Sunny	Yes	
Overcast	Yes	
Rainy	No	
Rainy	No	
Sunny	Yes	
Rainy	Yes	
Sunny	No	
Overcast	Yes	
Overcast	Yes	
Rainy	No	

Frequency Table		
Weather	No	Yes
Overcast		4
Rainy	3	2
Sunny	2	3
Grand Total	5	9

Like	elihood tab	le		
Weather	No	Yes		
Overcast		4	=4/14	0.29
Rainy	3	2	=5/14	0.36
Sunny	2	3	=5/14	0.36
All	5	9		
2.	=5/14	=9/14		
	0.36	0.64		



Problem: Players will play if weather is sunny. Is this statement is correct?

```
P(Yes | Sunny) = P( Sunny | Yes) * P(Yes) / P (Sunny)
Here we have
    P (Sunny |Yes) = 3/9 = 0.33,
    P(Sunny) = 5/14 = 0.36,
    P(Yes) = 9/14 = 0.64
```

Weather	Play
Sunny	No
Overcast	Yes
Rainy	Yes
Sunny	Yes
Sunny	Yes
Overcast	Yes
Rainy	No
Rainy	No
Sunny	Yes
Rainy	Yes
Sunny	No
Overcast	Yes
Overcast	Yes
Rainy	No

Frequency Table		
Weather	No	Yes
Overcast		4
Rainy	3	2
Sunny	2	3
Grand Total	5	9

Likelihood table				
Weather	No	Yes		
Overcast		4	=4/14	0.29
Rainy	3	2	=5/14	0.36
Sunny	2	3	=5/14	0.36
All	5	9		
	=5/14	=9/14		
	0.36	0.64		



Problem: Players will play if weather is sunny. Is this statement is correct?

P(Yes Sunny) = P(Sunny Yes) * P(Yes) / P (Sunny)
Here we have
P (Sunny Yes) = 3/9 = 0.33,
P(Sunny) = 5/14 = 0.36,
P(Yes) = 9/14 = 0.64
Now, P (Yes Sunny) = 0.33 * 0.64 / 0.36 = 0.60, (high probability)

Weather	Play	
Sunny	No	
Overcast	Yes	
Rainy	Yes	
Sunny	Yes	
Sunny	Yes	
Overcast	Yes	
Rainy	No	
Rainy	No	
Sunny	Yes	
Rainy	Yes	
Sunny	No	
Overcast	Yes	
Overcast	Yes	
Rainy	No	

Frequency Table				
Weather	No	Yes		
Overcast		4		
Rainy	3	2		
Sunny	2	3		
Grand Total	5	9		

Likelihood table				
Weather	No	Yes		
Overcast		4	=4/14	0.29
Rainy	3	2	=5/14	0.36
Sunny	2	3	=5/14	0.36
All	5	9		
	=5/14	=9/14		
	0.36	0.64		



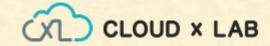
Problem: Players will play if weather is sunny. Is this statement is correct?

P(No | Sunny) = P(Sunny | No) * P(No) / P (Sunny)
Here we have
 P (Sunny |No) = 2/5 = 0.4,
 P(Sunny) = 5/14 = 0.36,
 P(No)= 5/14 = 0.36
Now, P (No | Sunny) = 0.4 * 0.36 / 0.36 = 0.40, (low probability)

Weather	Play	
Sunny	No	
Overcast	Yes	
Rainy	Yes	
Sunny	Yes	
Sunny	Yes	
Overcast	Yes	
Rainy	No	
Rainy	No	
Sunny	Yes	
Rainy	Yes	
Sunny	No	
Overcast	Yes	
Overcast	Yes	
Rainy	No	

Frequency Table				
Weather	No	Yes		
Overcast		4		
Rainy	3	2		
Sunny	2	3		
Grand Total	5	9		

Likelihood table				
Weather	No	Yes		
Overcast		4	=4/14	0.29
Rainy	3	2	=5/14	0.36
Sunny	2	3	=5/14	0.36
All	5	9		
	=5/14	=9/14		
	0.36	0.64		

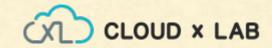


For Outlook = Rainy, Temp = Mild, Humidity = Normal, Windy = True, YES or No?

Outlook	Temp	Humidity	Windy	Play Golf
Rainy	Hot	High	False	No
Rainy	Hot	High	True	No
Overcast	Hot	High	False	Yes
Sunny	Mild	High	False	Yes
Sunny	Cool	Normal	False	Yes
Sunny	Cool	Normal	True	No
Overcast	Cool	Normal	True	Yes
Rainy	Mild	High	False	No
Rainy	Cool	Normal	False	Yes
Sunny	Mild	Normal	False	Yes
Rainy	Mild	Normal	True	Yes
Overcast	Mild	High	True	Yes
Overcast	Hot	Normal	False	Yes
Sunny	Mild	High	True	No
Rainy	Mild	Normal	True	???

Problem2:





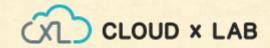
Lets prepare frequency tables of each feature

Frequency Tables

+		Play Golf		
×		Yes No		
Outlook	Sunny	3 3/9	2 2/5	
	Overcast	4 4/9	0 0/5	
	Rainy	2 2/9	33/5	

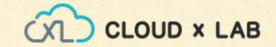
		Play Golf		
		Yes	No	
Temp.	Hot	2 2/9	2 2/5	
	Mild	44/9	2 2/5	
	Cool	33/9	11/5	

		Play G	iolf	Play G		Golf	
		Yes	No			Yes	No
I to a to be a	High	3 3/9	44/9	Windy	False	66/9	2 2/5
Humidity	Normal	6 6/9	11/5		Windy	True	3 3/9



-		Play	Golf			Play G	iolf	
×		Yes	No			Yes	No	
	Sunny	3 3/9	2 2/5	Temp.	Hot	2 2/9	2 2/5	
Outlook	Overcast	4 4/9	0 0/5		Mild	44/9	2 2/5	
	Rainy	2 2/9	33/5		Cool	33/9	11/5	
		Play Golf					Play Golf	
		Yes	No			Yes	No	
	High	3 3/9	44/9	Windy	False	66/9	2 2/5	
Humidity	Normal	6 6/9	11/5		True	3 3/9	33/5	

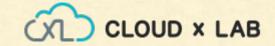
Problem2: For Outlook = Rainy, Temp = Mild, Humidity = Normal, Windy = True, YES or No?



-	+		Golf			Play G	iolf
×		Yes	No			Yes	No
	Sunny	3 3/9	2 2/5	Temp.	Hot	2 2/9	2 2/5
Outlook	Overcast	4 4/9	0 0/5		Mild	44/9	2 2/5
	Rainy	2 2/9	33/5		Cool	33/9	11/5
			Play Golf			Play Golf	
	_	Yes	No			Yes	No
	High	3 3/9	44/9	Windy	False	66/9	2 2/5
Humidity	Normal	6 6/9	11/5		True	3 3/9	33/5

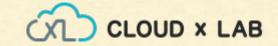
Problem2: For Outlook = Rainy, Temp = Mild, Humidity = Normal, Windy = True, YES or No?

Likelihood of yes = P(Outlook = Rainy|Yes) * P(Temp = Mild| Yes) * P(Humidity = Normal|Yes)*P(Windy = True|Yes)*P(Yes) = ?



-	+		Golf			Play G	iolf
×		Yes	No			Yes	No
	Sunny	3 3/9	2 2/5	Temp.	Hot	2 2/9	2 2/5
Outlook	Overcast	4 4/9	0 0/5		Mild	44/9	2 2/5
	Rainy	2 2/9	33/5		Cool	33/9	11/5
			Play Golf			Play G	iolf
	_	Yes	No			Yes	No
	High	3 3/9	44/9		False	66/9	2 2/5
Humidity	Normal	6 6/9	11/5	Windy	True	3 3/9	33/5

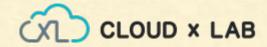
Problem2: For Outlook = Rainy, Temp = Mild, Humidity = Normal, Windy = True, YES or No?



-	+		Golf			Play G	iolf	
×		Yes	No			Yes	No	
	Sunny	3 3/9	2 2/5	Temp.	Hot	2 2/9	2 2/5	
Outlook	Overcast	4 4/9	0 0/5		Mild	44/9	2 2/5	
	Rainy	2 2/9	33/5		Cool	33/9	11/5	
			Play Golf				Play Golf	
		Yes	No			Yes	No	
the state	High	3 3/9	44/9	Windy	False	66/9	2 2/5	
Humidity	Normal	6 6/9	11/5		True	3 3/9	33/5	

Problem2: For Outlook = Rainy, Temp = Mild, Humidity = Normal, Windy = True, YES or No?

Likelihood of No = P(Outlook = Rainy|No) * P(Temp = Mild| No) * P(Humidity = Normal|No)*P(Windy = True|No)*P(No) = 3/5 * 2/5 * 1/5 * 3/5 * 5/14= 0.0103



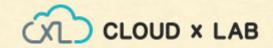
-	+		Golf			Play G	iolf
×		Yes	No			Yes	No
	Sunny	3 3/9	2 2/5	Temp.	Hot	2 2/9	2 2/5
Outlook	Overcast	4 4/9	0 0/5		Mild	44/9	2 2/5
	Rainy	2 2/9	33/5		Cool	33/9	11/5
		Play Golf					iolf
	_	Yes	No			Yes	No
	High	3 3/9	44/9	Windy	False	66/9	2 2/5
Humidity	Normal	6 6/9	11/5		True	3 3/9	33/5

Problem2: For Outlook = Rainy, Temp = Mild, Humidity = Normal, Windy = True, YES or No?

Likelihood of yes = **0.0141** Likelihood of No = **0.0103**

After Normalizaion, Yes = 0.0|4| / (0.0|4| + 0.0|03) = 0.58

 $N_0 = 0.0103 / (0.0141 + 0.0103) = 0.42$



-		Play	Golf			Play G	iolf
*		Yes	No			Yes	No
	Sunny	3 3/9	2 2/5	Temp.	Hot	2 2/9	2 2/5
Outlook	Overcast	4 4/9	0 0/5		Mild	44/9	2 2/5
	Rainy	2 2/9	33/5		Cool	33/9	11/5
			Play Golf			Play Golf	
		Yes	No			Yes	No
	High	3 3/9	44/9	Windy	False	66/9	2 2/5
Humidity	Normal	6 6/9	11/5		True	3 3/9	33/5

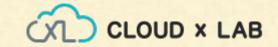
Problem2: For Outlook = Rainy, Temp = Mild, Humidity = Normal, Windy = True, YES or No?

YES



Zero Frequency Problem

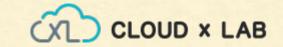
What if any of the count is 0??



Zero Frequency Problem

What if any of the count is 0?

- Add I to all counts
- It is a form of Laplace smoothing
- See https://en.wikipedia.org/wiki/Additive_smoothing



Using Python

```
#Import Library of Gaussian Naive Bayes model
from sklearn.naive_bayes import GaussianNB
import numpy as np
```

```
#assigning predictor and target variables
X= np.array([[-3,7],[1,5], [1,2], [-2,0], [2,3], [-4,0], [-1,1], [1,1], [-2,2], [2,7], [-4,1],
[-2,7]])
y = np.array([3, 3, 3, 3, 4, 3, 3, 4, 3, 4, 4, 4])
#Create a Gaussian Classifier
model = GaussianNB()
```

Train the model using the training sets
model.fit(X, y)

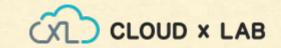
```
#Predict Output
predicted= model.predict([[1,2],[3,4]])
print(predicted)
```

See the Jupyter Notebook.



Tips to improve the Naive Bayes Model

- If continuous features do not have normal distribution,
 - we should use transformation or different methods to convert
- If test data set has zero frequency issue,
 - apply smoothing techniques "Laplace smoothing"
- Remove correlated features,
 - as the highly correlated features are voted twice in the model
 and it can lead to over inflating importance.
- And it can lead to over innating importance.
 Native Device electifice has limited actions for comment
- Naive Bayes classifier has limited options for parameter tuning
- Can't be ensembled because there is no variance to reduce



Variants

Gaussian:

• It is used in classification and it assumes that features follow a normal distribution.

Multinomial:

It is used for discrete counts.

Implements the naive Bayes algorithm for multinomially distributed data It is one of the two classic naive Bayes variants used in text classification

Bernoulli:

The binomial model is useful if your feature vectors are binary (i.e. zeros and ones).
One application would be text classification with 'bag of words' model where the Is & 0s are "word occurs in the document" and "word does not occur in the document" respectively.

http://scikit-learn.org/stable/modules/naive_bayes.html



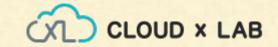
Applications

I. Real time Prediction:

Naive Bayes is an eager learning classifier and it is sure fast.
 Thus, it could be used for making predictions in real time.

2. Multi class Prediction:

• Well known for multi class prediction feature.



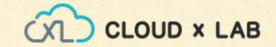
Applications

1. Text classification/ Spam Filtering/ Sentiment Analysis:

- Mostly used in text classification
- Have higher success rate as compared to other algorithms.
- Widely used in Spam filtering (identify spam e-mail)
- and Sentiment Analysis

2. Recommendation System:

 Naive Bayes Classifier and Collaborative Filtering together builds a Recommendation System that uses machine learning and data mining techniques to filter unseen information and predict whether a user would like a given resource or not



Further references

- http://scikit-learn.org/stable/modules/naive_bayes.html
- https://en.wikipedia.org/wiki/Bayes%27_theorem
- https://en.wikipedia.org/wiki/Naive_Bayes_classifier





Naive Bayes

Thank you! reachus@cloudxlab.com

