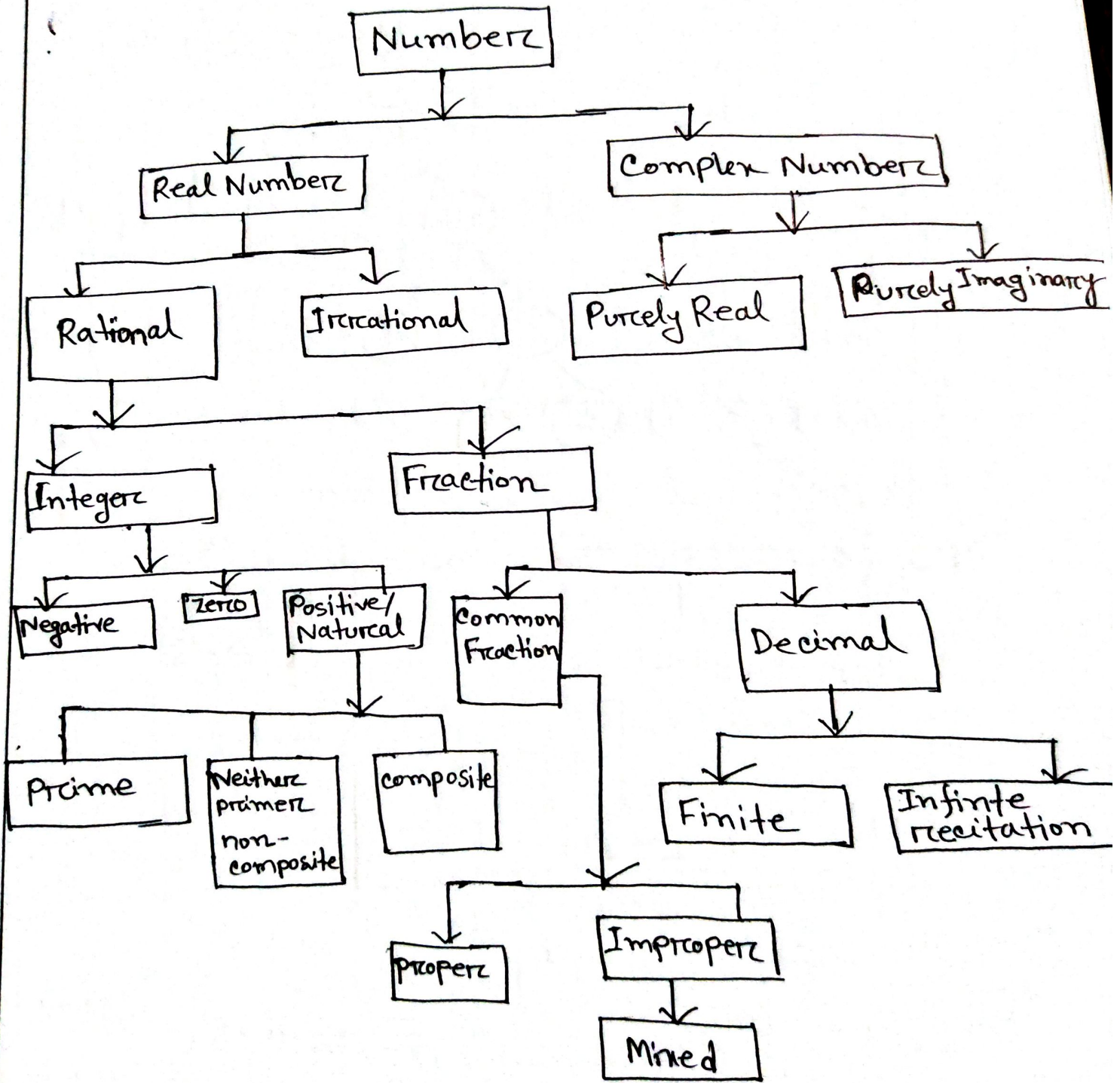
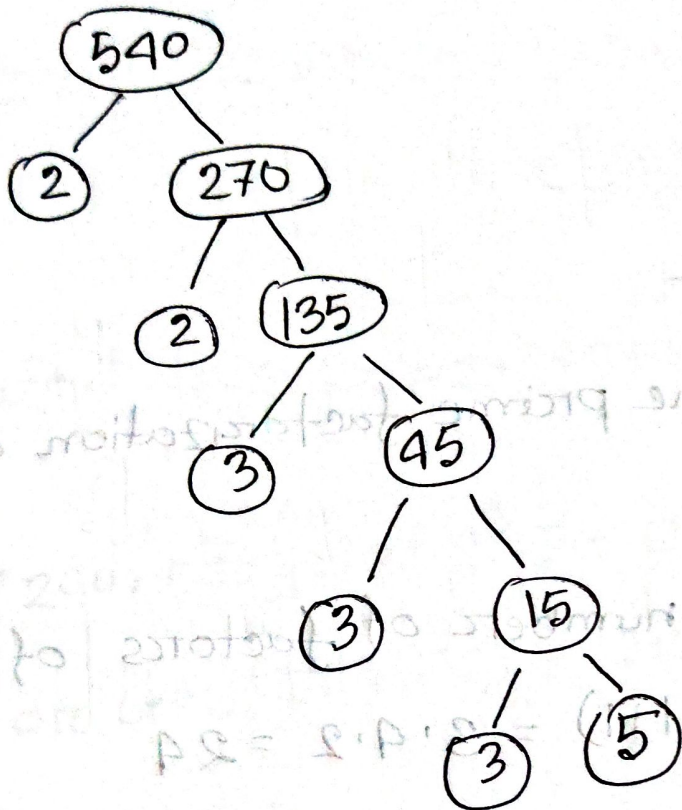


1. Classification of number system:



②



Therefore, the prime factorization of 540

$$is = 2^2 \cdot 3^3 \cdot 5.$$

③

$$\begin{array}{r} 2 \overline{)540} \\ 2 \overline{)270} \\ 3 \overline{)135} \\ 3 \overline{)45} \\ 3 \overline{)15} \\ 5 \end{array}$$

Therefore, the prime factorization of 540 is $= 2^2 \cdot 3^3 \cdot 5$.

So, the total number of factors of 540 is

$$(2+1)(3+1)(1+1) = 3 \cdot 4 \cdot 2 = 24$$

Calculation for all factors -

$$540 = 1 \times 540$$

$$= 2 \times 270$$

$$= 3 \times 180$$

$$= 4 \times 135$$

$$= 5 \times 108$$

$$= 6 \times 90$$

$$= 9 \times 60$$

$$= 10 \times 54$$

$$= 12 \times 45$$

$$= 15 \times 36$$

$$= 18 \times 30$$

$$= 20 \times 27$$

\therefore The all factors of 540 are :- 1, 2, 3, 4, 5, 6, 9, 10, 12, 15, 18, 20, 27, 30, 36, 45, 54, 60, 90, 180, 135, 180, 270 and 540.

4

$$240 = 2 \times 120 = 2 \times 2 \times 60 = 2 \times 2 \times 2 \times 30 = 2 \times 2 \times 2 \times 2 \times 15 \\ = 2^4 \times 3 \times 5$$

$$540 = 2 \times 270 = 2 \times 2 \times 135 = 2 \times 2 \times 3 \times 45 = 2 \times 2 \times 3 \times 3 \times 15 = 2^2 \times 3^3 \times 5$$

$$\therefore \text{LCM}(240, 540) = 2^4 \cdot 3^3 \cdot 5 = 2160$$

$$\& \text{HCF or GCD}(240, 540) = 2 \cdot 3 \cdot 5 = 30$$

5

$$42 = 2 \times 21 = 2 \times 3 \times 7$$

$$63 = 3 \times 21 = 3 \times 3 \times 7 = 3^2 \times 7$$

$$140 = 2 \times 70 = 2 \times 2 \times 35 = 2^2 \times 5 \times 7$$

$$\therefore \text{LCM}(42, 63, 140) = 2^2 \times 3^2 \times 5 \times 7 = 1260$$

$$\& \text{HCF}(42, 63, 140) = 2 \times 7 = 14$$

(6)

Calculation for

Numberators

$$2 = 2^1$$

$$8 = 2^3$$

$$16 = 2^4$$

$$10 = 2^1 \times 5^1$$

~~Calculation~~

Calculation for Denominators

$$3 = 3^1$$

$$9 = 3^2$$

$$81 = 3^4$$

$$27 = 3^3$$

$$\text{LCM}(3, 9, 81, 27) = 3^4 = 81$$

$$\begin{aligned} \text{LCM}(2, 8, 16, 10) &= 2^4 \times 5 \\ &= 80 \end{aligned}$$

$$\text{HCF}(3, 9, 81, 27) = 3$$

$$\text{HCF}(2, 8, 16, 10) = 2$$

$$\text{HCF of } \frac{2}{3}, \frac{8}{9}, \frac{16}{81}, \frac{10}{27} = \frac{\text{HCF}(2, 8, 16, 10)}{\text{LCM}(3, 9, 81, 27)} = \frac{2}{81}$$

$$\text{LCM of } \frac{2}{3}, \frac{8}{9}, \frac{16}{81} \text{ and } \frac{10}{27} = \frac{\text{HCF LCM}(2, 8, 16, 10)}{\text{HCF}(3, 9, 81, 27)} = \frac{80}{3}$$

(7)

We have, $\frac{1+\sqrt{3}i}{1-\sqrt{3}i}$

$$= \frac{(1+\sqrt{3}i)(1+\sqrt{3}i)}{(1-\sqrt{3}i)(1+\sqrt{3}i)}$$
$$= \frac{1+2\sqrt{3}i-3}{1^2-(\sqrt{3}i)^2}$$
$$= \frac{-2+2\sqrt{3}i}{-1+3}$$
$$= \frac{2(-1+\sqrt{3}i)}{2}$$
$$= \frac{-1+\sqrt{3}i}{1}$$

Let $z = -\frac{1}{2} + \frac{\sqrt{3}}{2}i$

$$|z| = \sqrt{\left(-\frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2}$$

$$r = \sqrt{\frac{1}{4} + \frac{3}{4}} = \sqrt{\frac{4}{4}} = 1$$

\therefore Modulus of z is $= 1$

And Argument of z will-

$$\theta = \pi - \tan^{-1} \left| \frac{\frac{\sqrt{3}}{2}}{\frac{1}{2}} \right|$$

$$= \pi - \tan^{-1}(\sqrt{3})$$

$$= \pi - \frac{\pi}{3}$$

$$= \frac{2\pi}{3}$$

Polar Form $-\frac{1}{2} + \frac{\sqrt{3}}{2}i$

Exponential form is $z = r e^{i\theta}$

$$= 1 \cdot e^{i \frac{2\pi}{3}}$$

$$= e^{\frac{2\pi}{3}i}$$

8

We have, $\sqrt{-16} \times \sqrt{-4}$

$$= \sqrt{16}i \times \sqrt{4}i$$

$$= 4i \times 2i$$

$$= 8i^2$$

$$= -8$$

and $\frac{\sqrt{-16}}{\sqrt{-4}} = \frac{4i}{2i} = 2$

9

We have, $z = 2 + i$

$$\therefore 8z - z^2 = 8(2+i) - (2+i)^2$$

$$= 16 + 8i - (4 + 4i + i^2)$$

$$= 16 + 8i - 4 - 4i + 1$$

$$= 13 + 4i$$

Modulus $|z| = \sqrt{(13)^2 + (4)^2}$

$$= \sqrt{169 + 16}$$

$$= \sqrt{185}$$

$$\therefore \theta = \tan^{-1} \frac{4}{13}$$

$$= 17.102^\circ$$

$$\textcircled{10} \text{ Let, } z = 1 + i\sqrt{3} \quad z = x + iy \quad |z| = \sqrt{x^2 + y^2}$$
$$\theta = \tan^{-1} \left| \frac{y}{x} \right|$$

$$\begin{aligned} \therefore \text{Modulus of } z &= \sqrt{(1)^2 + (\sqrt{3})^2} \\ &= \sqrt{1+3} \\ &= \sqrt{4} \\ &= 2 \end{aligned}$$

$$\therefore r = 2$$

$$\begin{aligned} \text{Argument of } z &= \tan^{-1} \left| \frac{y}{x} \right| \\ &= \tan^{-1} \left| \frac{\sqrt{3}}{1} \right| \\ &= \tan^{-1} \tan \frac{\pi}{3} \\ &= \frac{\pi}{3} \end{aligned}$$

Therefore, $r(\cos\theta + i\sin\theta)$ form is

$$= 2 \left(\cos \frac{\pi}{3} + i \sin \frac{\pi}{3} \right).$$