

1. Number system classification.

There are two types of number system: ① Real numbers,
② Complex number.

Two types of Real numbers: ① Rational,
② Irrational.

There are two types of rational number: ① Integer,
② Fraction.

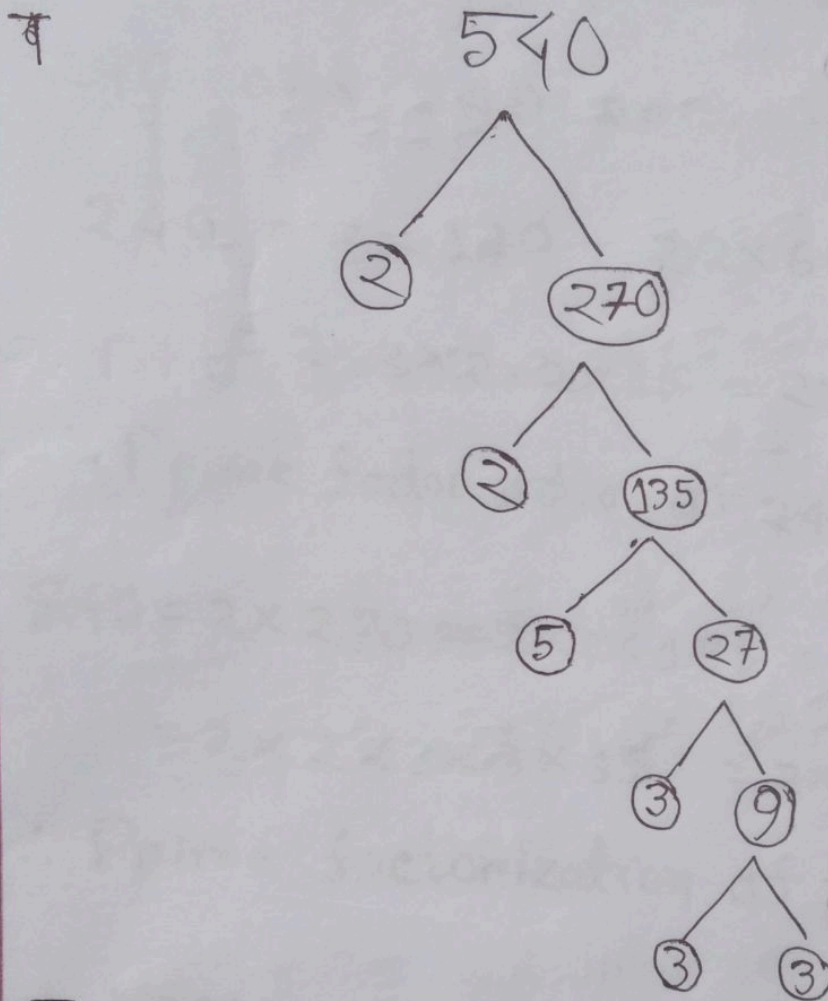
The Integer have three types:

① Negative.

② Zero.

③ Positive.

2. Find the prime factorization of 540 using tree diagram.



Therefore the prime factorization of

$$540 = 2^2 \cdot 5 \cdot 3^3$$

∴ All the prime factors of 540 = 2, 3, 5

3. Find all the factors of 540

$$540 = 1 \times 540$$

$$= 2 \times 270$$

$$= 4 \times 135$$

$$= 5 \times 108$$

$$= 10 \times 54$$

$$= 20 \times 27$$

$$= 3 \times 180$$

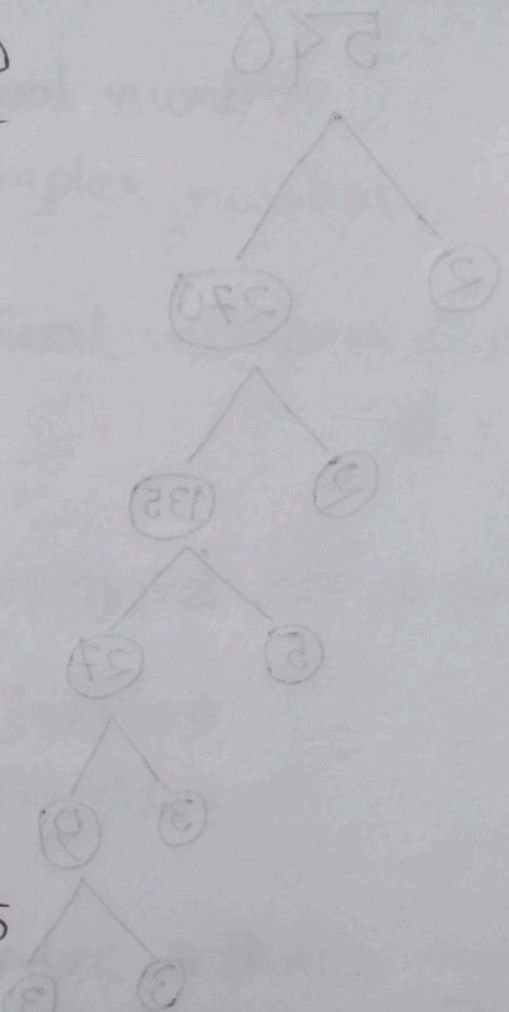
$$= 6 \times 90$$

$$= 12 \times 45$$

$$= 9 \times 60$$

$$= 18 \times 30$$

$$= 36 \times 15$$



Now, All the factors of 540 = 1, 2, 3, 4, 5, 6, 9, 10, 12, 15, 18, 20, 27, 30, 36, 45, 54, 60, 90, 108, 135, 180, 270, 540

4. Given numbers are 240 and 540

Therefore, the prime factorization of

240 and 540 are,

$$240 = 2 \times 120 = 2 \times 2 \times 60 = 2 \times 2 \times 2 \times 30$$

$$= 2 \times 2 \times 2 \times 2 \times 15 = 2 \times 2 \times 2 \times 2 \times 3 \times 5$$

\therefore Prime factorization of 240 = $2^4 \cdot 3 \cdot 5$

$$540 = 2 \times 270 = 2 \times 2 \times 135 = 2 \times 2 \times 3 \times 45$$

$$= 2 \times 2 \times 3 \times 3 \times 15 = 2 \times 2 \times 3 \times 3 \times 3 \times 5$$

\therefore Prime factorization of 540 = $2^2 \cdot 3^3 \cdot 5$

$$\therefore \text{LCM of } (240, 540) = 2^4 \times 3^3 \times 5 = 2160$$

$$\therefore \text{GCD of } (240, 540) = 2^2 \times 3 \times 5 = 60$$

5. Given numbers are; 42, 63 and 140

The prime factorization of 42, 63, and 140 are,

$$42 = 2 \times 21 = 2 \times 3 \times 7 \quad \therefore 42 = 2 \cdot 3 \cdot 7$$

$$63 = 3 \times 21 = 3 \times 3 \times 7 \quad \therefore 63 = 3^2 \cdot 7$$

$$140 = 2 \times 70 = 2 \times 2 \times 35 = 2 \times 2 \times 5 \times 7$$

$$\therefore 140 = 2^2 \cdot 5 \cdot 7$$

$$\therefore \text{HCF of } (42, 63, 140) = 7$$

$$\therefore \text{LCM of } (42, 63, 140) = 2^2 \times 3^2 \times 5 \times 7$$

$$= 1260$$

6. The Given numbers are, $\frac{2}{3}$, $\frac{8}{9}$, $\frac{16}{81}$, $\frac{10}{27}$

Example

Calculation of numerators

$$2 = 2^1$$

$$8 = 2^3$$

$$16 = 2^4$$

$$10 = 2 \cdot 5$$

$$\therefore \text{LCM of } (2, 8, 16, 10) = 2^4 \times 5$$

$$\therefore \text{HCF of } (2, 8, 16, 10) = 2$$

$$= 80$$

Calculation of Denominators,

$$3 = 3^1$$

$$9 = 3^2$$

$$81 = 3^4$$

$$27 = 3^3$$

$$\therefore \text{LCM of } (3, 9, 81, 27) = 3^4 = 81$$

$$\therefore \text{HCF of } (3, 9, 81, 27) = 3^1 = 3$$

$$\therefore \text{HCF of } \left(\frac{2}{3}, \frac{8}{9}, \frac{16}{81}, \frac{10}{27} \right) = \frac{\text{HCF of nominator}}{\text{LCM of Denominator}}$$
$$= \frac{2}{81}$$

$$\therefore \text{LCM of } \left(\frac{2}{3}, \frac{8}{9}, \frac{16}{81}, \frac{10}{27} \right) = \frac{\text{LCM of nominator}}{\text{HCF of Denominator}}$$
$$= \frac{80}{3}$$

7. Given, $z = \frac{1 + \sqrt{3}i}{1 - \sqrt{3}i}$

Find the modulus of z :

Notation: $|z|$

Rule: $|z| = \sqrt{x^2 + y^2}$

Now, $z = \frac{\sqrt{(1)^2 + (\sqrt{3})^2}}{\sqrt{(1)^2 + (-\sqrt{3})^2}}$

$$= \frac{\sqrt{4}}{\sqrt{4}}$$

$$= 1 \text{ Ans.}$$

again,

Suppose $z_1 = 1 + \sqrt{3}i$

$$z_2 = 1 - \sqrt{3}i$$

$$\begin{aligned} \therefore z_1 \text{ Argument is } \theta_1 &= \tan^{-1} \frac{y}{x} \\ &= \tan^{-1} \frac{\sqrt{3}}{1} \\ &= 60^\circ \end{aligned}$$

And, z_2 Argument is $\theta_2 = 360^\circ - \tan^{-1} \frac{y}{x}$

$$= 360^\circ - \tan^{-1} \frac{\sqrt{3}}{1}$$

$$= 360^\circ - 60^\circ$$
$$= 300^\circ$$

\therefore Argument of $z = \frac{60^\circ}{300^\circ} = 5^\circ$

The polar form of $z = (r, \theta)$

$$= (1, 5^\circ)$$

8. Given numbers are $\sqrt{6}$, $\sqrt{-16}$ and $\sqrt{-4}$

$$\begin{aligned} \text{Evaluate of } \sqrt{-16} \times \sqrt{-4} &= \sqrt{-4^2} \times \sqrt{-2^2} \\ &= (-4) \times (-2) \\ &= 8 \text{ (Ans)} \end{aligned}$$

$$\begin{aligned} \text{Evaluate of } \frac{\sqrt{-16}}{\sqrt{-4}} &= \frac{-4}{-2} = 2 \\ &\text{ (Ans)} \end{aligned}$$

9. Given, $Z = 2 + i$

$$\begin{aligned} \text{Now, modulus of } 8z - z^2 &= 8(2+i) - (2+i)^2 \\ &= 16 + 8i - 4 - 4i - i^2 \\ &= 13 + 4i \end{aligned}$$

$$\therefore r = \sqrt{13^2 + 4^2} = \sqrt{169 + 16} = \sqrt{185} \text{ (Ans)}$$

$$\therefore \theta = \tan^{-1} \frac{4}{13}$$

10. Given, $z = 1 + i\sqrt{3}$

Notation: $|-|z|$

Rule: $|z| = \sqrt{x^2 + y^2}$

Now, $|z| = \sqrt{1^2 + (\sqrt{3})^2}$

$$= \sqrt{4}$$

$$= 2$$

And, $\theta = \tan^{-1} \frac{\sqrt{3}}{1}$

$$= \tan^{-1} \tan 60^\circ$$

$$= 60^\circ$$

$\therefore |z| = (r, \theta)$

$$= (2, 60^\circ)$$

Ans: