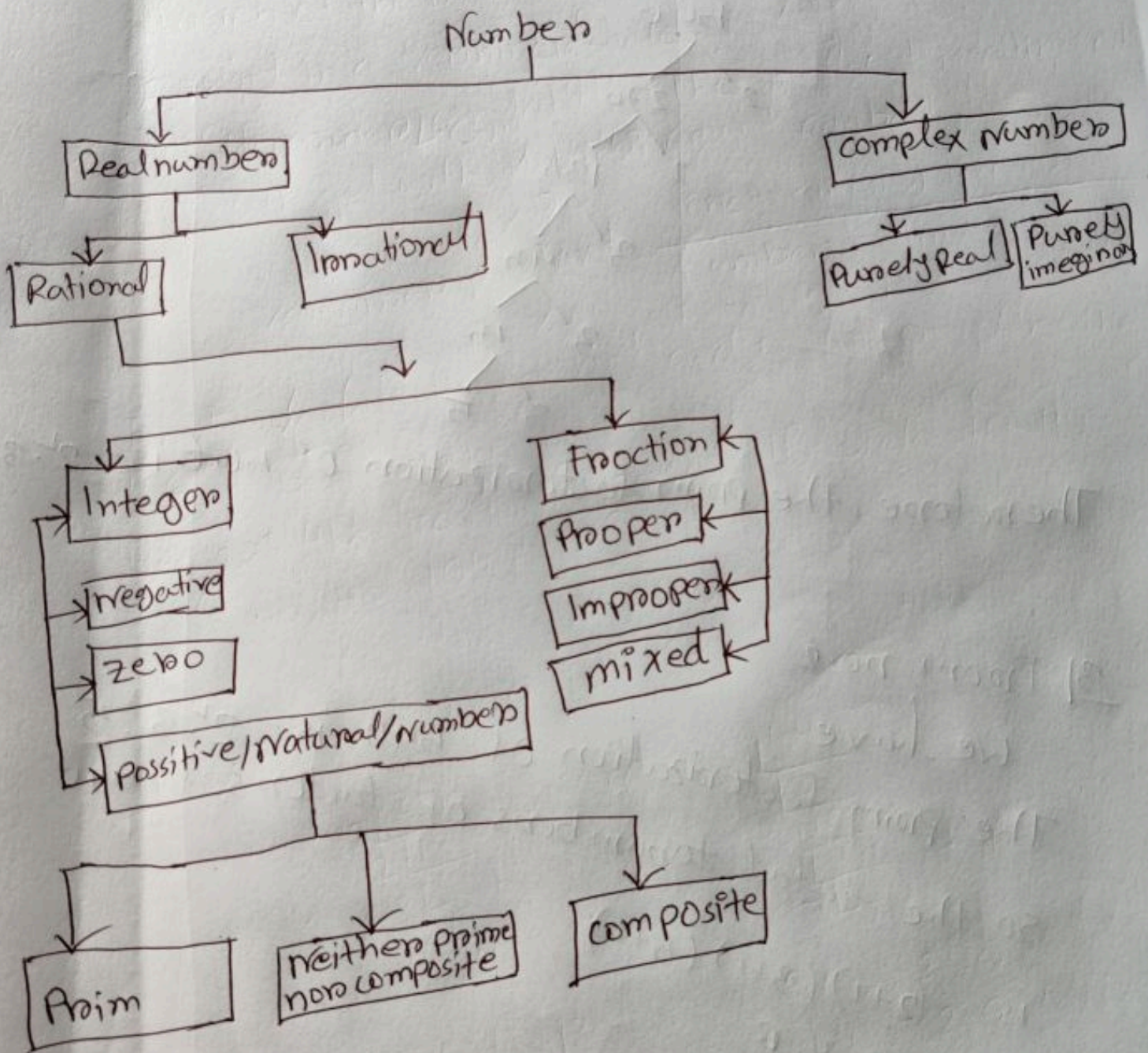
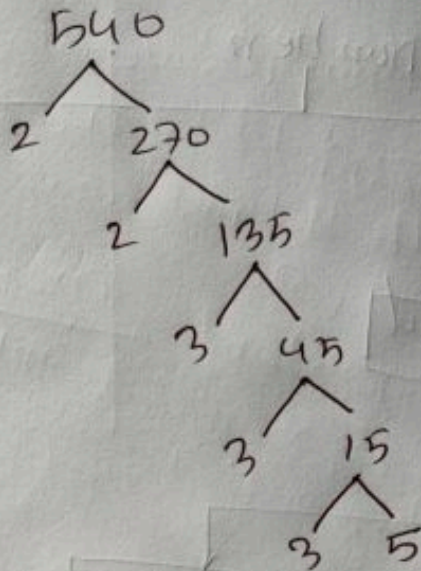


1. classification of number system



21 Prim factorization of 540:



Therefore, the prim factorization of 540 is $= 2^2 \cdot 3^3 \cdot 5$

3) From no. 2

We have

The prim factorization of 540 is $= 2^2 \cdot 3^3 \cdot 5$

So, the total numbers of factors of 540

$$\begin{aligned} \text{is} &= (2+1)(3+1)(5+1) \\ &= 3 \cdot 4 \cdot 6 \\ &= 24 \end{aligned}$$

Calculation for all factors:

$$540 = 1 \times 540$$

$$= 2 \times 270$$

$$= 3 \times 180$$

$$= 4 \times 135$$

$$= 5 \times 108$$

$$= 6 \times 90$$

$$= 9 \times 60$$

$$= 10 \times 60$$

$$= 12 \times 45$$

$$= 15 \times 36$$

$$= 18 \times 30$$

$$= 20 \times 27$$

The factors of 540 are:

1, 2, 3, 4, 5, 6, 9, 10, 12, 15, 18, 20, 27, 30, 36, 45, 54,
60, 90, 108, 135, 180, 270, 540

4) GCD and LCM of 240 and 540:

$$\begin{array}{r} 2 \overline{) 240} \\ \underline{2 \overline{) 120}} \\ \underline{2 \overline{) 60}} \\ \underline{2 \overline{) 30}} \\ \underline{3 \overline{) 15}} \\ 5 \end{array}$$

$$\text{and } \begin{array}{r} 2 \overline{) 540} \\ \underline{2 \overline{) 270}} \\ \underline{3 \overline{) 135}} \\ \underline{3 \overline{) 45}} \\ \underline{3 \overline{) 15}} \\ 5 \end{array}$$

\therefore Prime factorization of 240 = $2^4 \cdot 3^1 \cdot 5^1$
and Prime factorization of 540 = $2^2 \cdot 3^3 \cdot 5^1$

$$\therefore \text{GCD of } (240, 540) = 2^2 \times 3 \times 5 \\ = 4 \times 3 \times 5 \\ = 60$$

$$\text{LCM of } (240, 540) = 2^4 \times 3^3 \times 5 \\ = 16 \times 27 \times 5 = 2160$$

5. H.C.F and L.C.m of 42, 63

$$\begin{array}{r} 2 \overline{) 42} \\ 3 \overline{) 21} \\ 7 \end{array}$$

$$= 2 \times 3 \times 7$$

$$\begin{array}{r} 3 \overline{) 63} \\ 3 \overline{) 21} \\ 7 \end{array}$$

$$= 3^2 \times 7$$

$$\begin{array}{r} 2 \overline{) 140} \\ 2 \overline{) 70} \\ 3 \overline{) 35} \\ 7 \end{array}$$

$$= 2^2 \times 5 \times 7$$

$$\therefore \text{H.C.F of } (42, 63, 140) = 7$$

$$\begin{aligned} \text{L.C.m of } (42, 63, 140) &= 2^2 \times 3^2 \times 7 \times 5 \\ &= 1260 \end{aligned}$$

06. calculation for numerators,

$$2 = 2^1$$

$$8 = 2^3$$

$$16 = 2^4$$

$$10 = 2^1 \times 5^1$$

Calculation for Denominators

$$3 = 3^1$$

$$9 = 3^2$$

$$81 = 3^4$$

$$27 = 3^3$$

$$\therefore \text{L.C.M.}(2, 8, 16, 10) = 2^4 \times 5 = 80$$

$$\therefore \text{H.C.F.}(2, 8, 16, 10) = 2$$

$$\therefore \text{L.C.M.}(3, 9, 81, 27) = 3^4 = 81$$

$$\text{H.C.F.}(3, 9, 81, 27) = 3$$

Here, H.C.F. of $\frac{2}{3}, \frac{8}{9}, \frac{16}{81}, \frac{10}{27}$

$$= \frac{\text{H.C.F.}(2, 8, 16, 10)}{\text{L.C.M.}(3, 9, 81, 27)}$$

$$= \frac{2}{81}$$

L.C.M of $\frac{2}{3}, \frac{8}{9}, \frac{16}{81}, \frac{10}{27}$

$$= \frac{\text{LCM}(2, 8, 16, 10)}{\text{HCF}(3, 9, 81, 27)}$$

$$= \frac{80}{3}$$

07. We have

$$\begin{aligned} & \frac{1 + \sqrt{3}i}{1 - \sqrt{3}i} \\ &= \frac{(1 + \sqrt{3}i)(1 + \sqrt{3}i)}{(1 - \sqrt{3}i)(1 + \sqrt{3}i)} \\ &= \frac{1 + 2\sqrt{3}i - 3}{1 - (\sqrt{3})^2} \\ &= \frac{-2 + 2\sqrt{3}i}{1 + 3} \\ &= \frac{2(-1 + \sqrt{3}i)}{4} \\ &= -\frac{1}{2} + \frac{\sqrt{3}}{2}i \end{aligned}$$

$$z = -\frac{1}{2} + \frac{\sqrt{3}}{2}i$$

$$|z| = \sqrt{\left(-\frac{1}{2}\right)^2 + \left(\frac{\sqrt{3}}{2}\right)^2}$$

$$r = \sqrt{\frac{1}{4} + \frac{3}{4}}$$

$$= \sqrt{\frac{4}{4}}$$

$$= 1$$

\therefore modulus of $z = 1$

\therefore Argument of z

$$\theta = \pi - \tan^{-1} \frac{\sqrt{3}/2}{1/2}$$

$$= \pi - \frac{\pi}{3}$$

$$= \frac{2\pi}{3}$$

polars form $1/2 + \frac{\sqrt{3}}{2}i$

$$\begin{aligned}\text{Exponential form is } z &= re^{i\theta} \\ &= 1 \cdot e^{i \cdot 2\pi/3} \\ &= e^{2\pi/3 i}\end{aligned}$$

08. we have

$$\begin{aligned}\sqrt{-16} \times \sqrt{-4} \\ &= \sqrt{16i} \times \sqrt{4i} \\ &= 4i \times 2i \\ &= 8i^2\end{aligned}$$

$$\begin{aligned}\text{and } \sqrt{-16}/\sqrt{-4} \\ &= \frac{4i}{2i} \\ &= 2\end{aligned}$$

09. we have

$$\begin{aligned}z &= 2+i \\ \therefore 8z - z^2 &= 8(2+i) - (2+i)^2 \\ &= 16 + 8i - (4 + 4i + i^2) \\ &= 16 + 8i - (4 + 4i + 1) \\ &= 13 + 4i\end{aligned}$$

$$\begin{aligned}\therefore \text{ modulus } r &= \sqrt{(13)^2 + (4)^2} \\ &= \sqrt{169 + 16} \\ &= \sqrt{185}\end{aligned}$$

$$\begin{aligned}\theta &= \tan^{-1} \frac{4}{13} \\ &= 17.102\end{aligned}$$

10. we have

$$z = 1 + i\sqrt{3} \quad z = x + iy \quad |z| = \sqrt{x^2 + y^2}$$

$$\theta = \tan^{-1} y/x$$

$$\therefore \text{modulus of } z = \sqrt{(1)^2 + (\sqrt{3})^2}$$
$$= \sqrt{1+3}$$
$$= 2$$

$$\therefore r = 2$$

$$\text{Argument of } z = \tan^{-1}(\sqrt{3}/1)$$
$$= \tan^{-1} \tan \pi/3$$
$$= \pi/3$$

$$\therefore \text{therefore, } r(\cos \theta + i \sin \theta) \text{ from is}$$
$$2(\cos \pi/3 + i \sin \pi/3).$$