



$$\begin{aligned}
 & \textcircled{2} \quad \frac{v_2 - 10}{40} + \frac{v_L - v_4}{30} + \frac{v_2 - v_4}{20} + v_2 - 5 = 0 \\
 \Rightarrow & \frac{3v_2 - 30 + 4v_L - 4v_4 + 6v_2 - 6v_4 + 120v_2 - 600}{120} = 0 \\
 \Rightarrow & 3v_2 - 30 + 4v_L + 6v_2 + 120v_2 - 600 = 0 \quad [v_4 = 0] \\
 \Rightarrow & 133v_2 - 630 = 0 \\
 \therefore v_2 &= 4.736
 \end{aligned}$$

$$\begin{aligned}
 v_3 - 5 + \frac{v_3}{10} &= 0 \\
 \Rightarrow \frac{10v_3 - 50 + v_3}{10} &= 0 \\
 \Rightarrow 10v_3 - 50 + v_3 &= 0 \\
 \Rightarrow 11v_3 &= 50 \\
 \therefore v_3 &= 4.545
 \end{aligned}$$

A

$$\textcircled{1} \quad \frac{\frac{v_1 - v_2}{40} + v_1 - 10}{\frac{10}{0.5}} = 0 \quad \textcircled{1}$$

$$\frac{v_2 - v_1}{40} + \frac{v_2 - 20}{20} + \frac{v_1}{10} = 0 \quad \textcircled{1}$$

$$\Rightarrow \left[ \frac{v_2 - v_1 + 2v_2 - 40 + 4v_1}{40} \right] = 0$$

$$\Rightarrow 7v_2 - v_1 - 40 = 0 \quad \textcircled{1}$$

From eqn-1,

$$\frac{v_1 - v_L}{40} + v_1 - 10 = 0$$

$$\Rightarrow \frac{v_1 - v_L + 40v_1 - 400}{40} = 0$$

$$\Rightarrow 41v_1 - v_L - 400 = 0$$

$$v_1 = 9.93$$

$$v_2 = 7.13 \quad \textcircled{2}$$