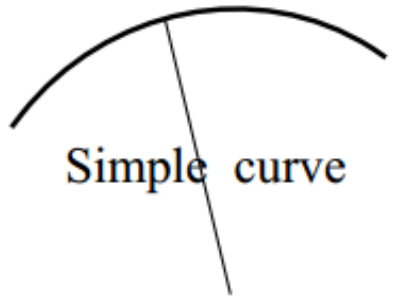


**CE-103**

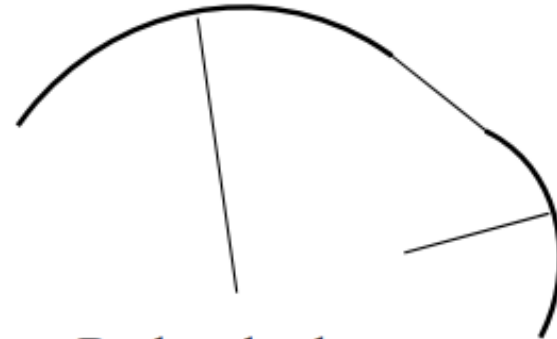
**Surveying**

**Lecture-11**

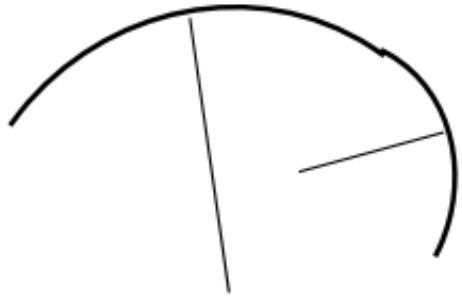
**Curve Surveying**



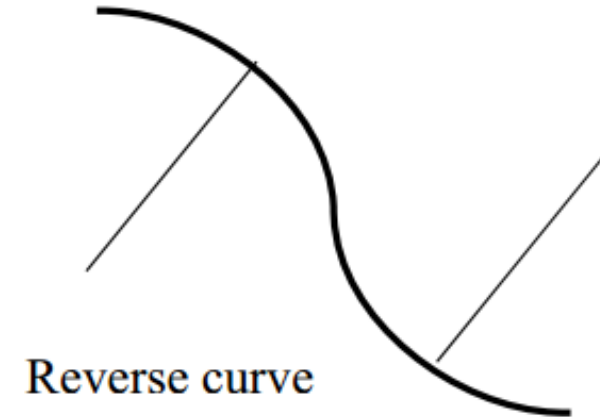
Simple curve



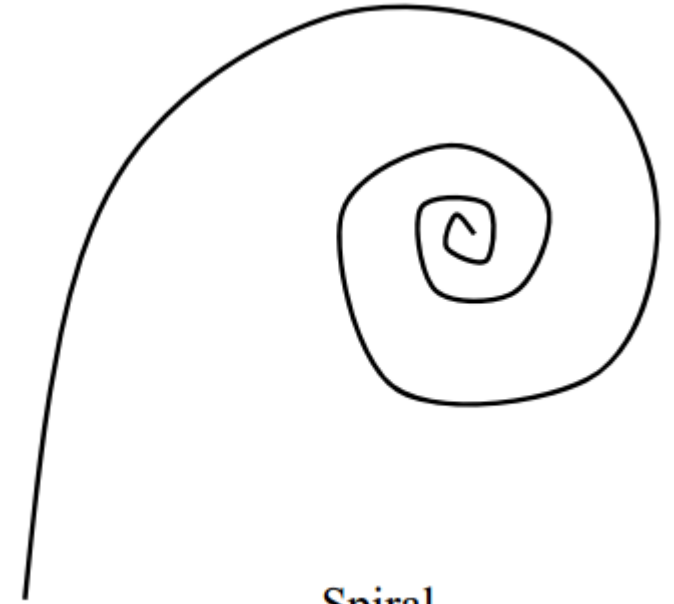
Broken-back curves



Compound curve

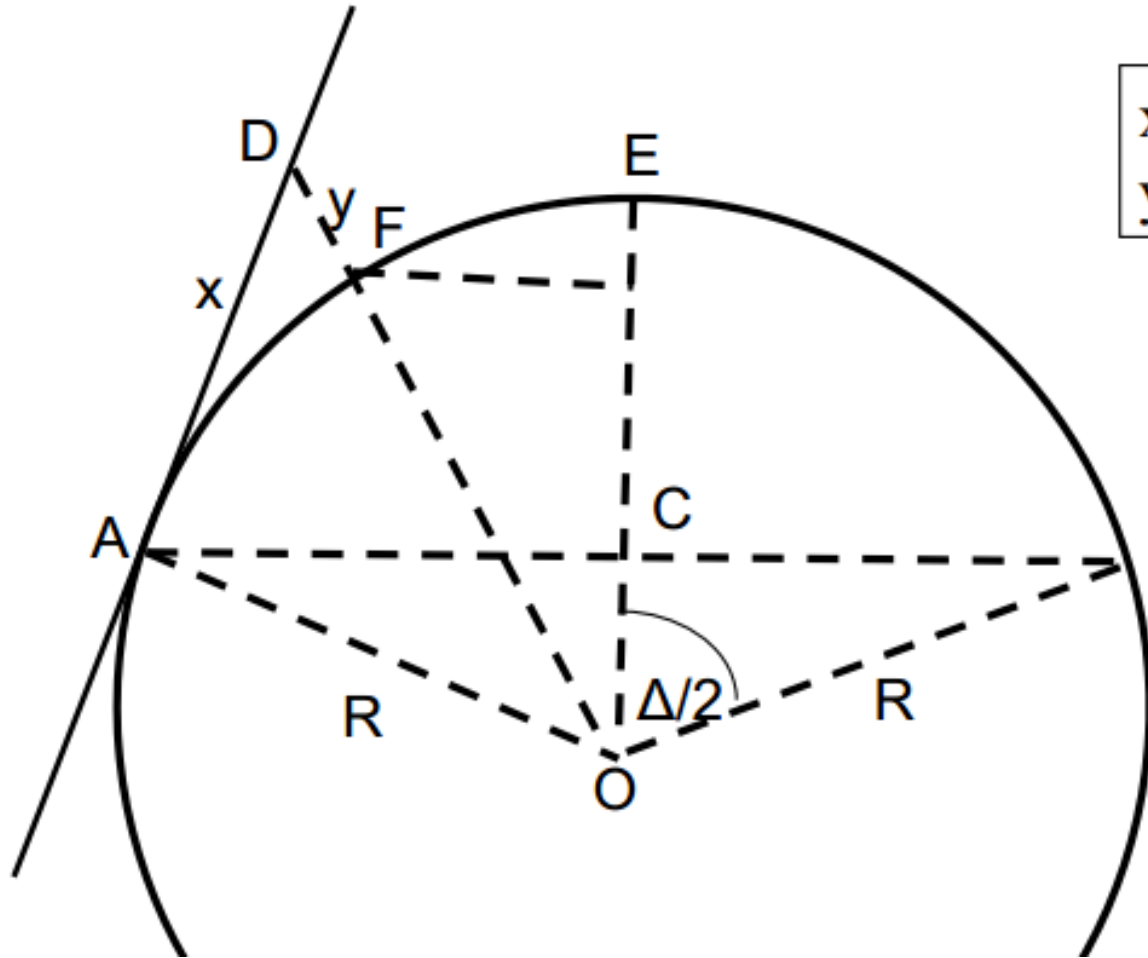


Reverse curve



Spiral

# Radial offset from tangent



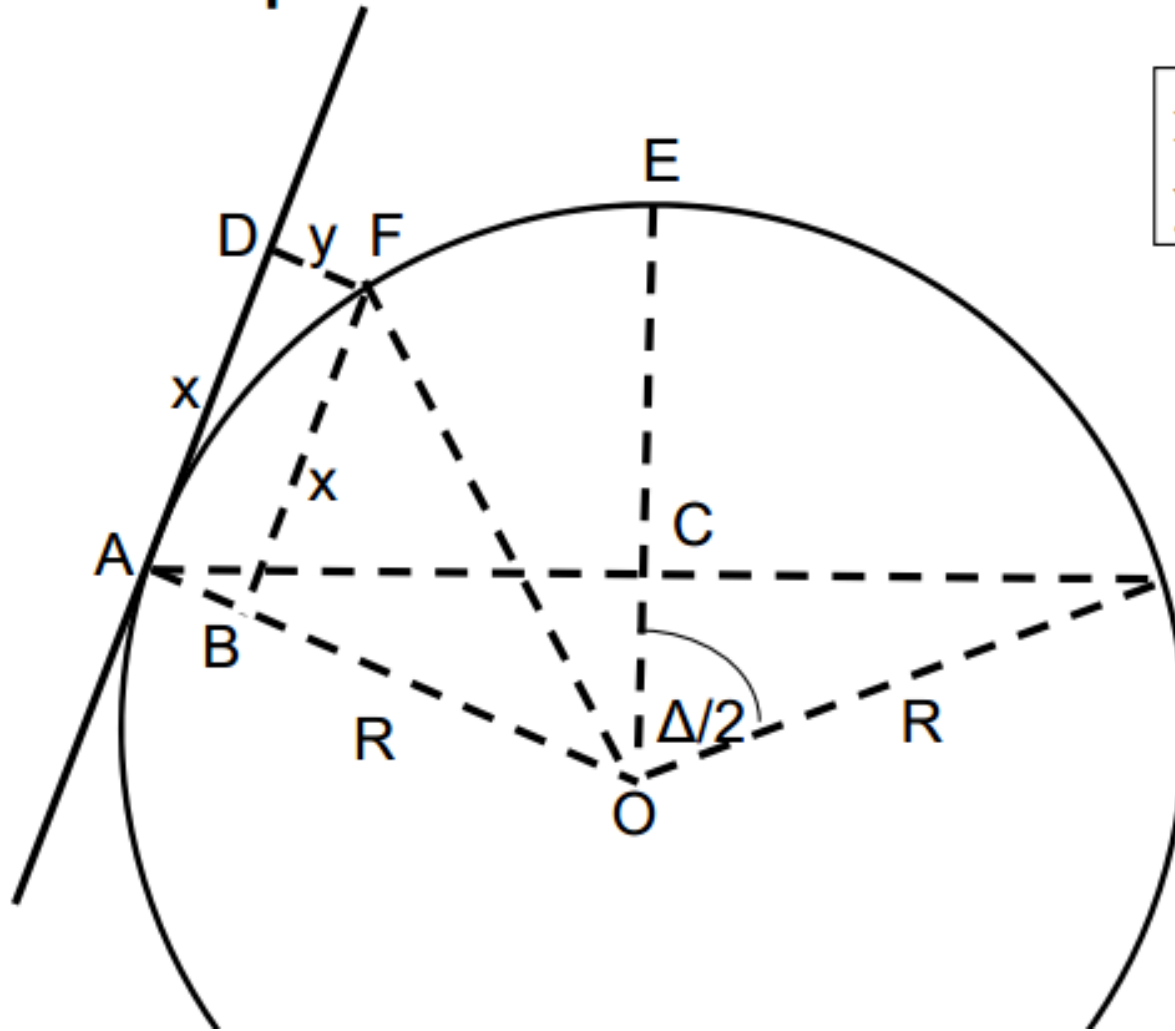
$x = \text{known}$   
 $y = ?$

$\Delta OAD \Rightarrow$

$$(R+y)^2 = x^2 + R^2$$

$$y = \sqrt{(x^2 + R^2)} - R$$

# Perpendicular offset from tangent



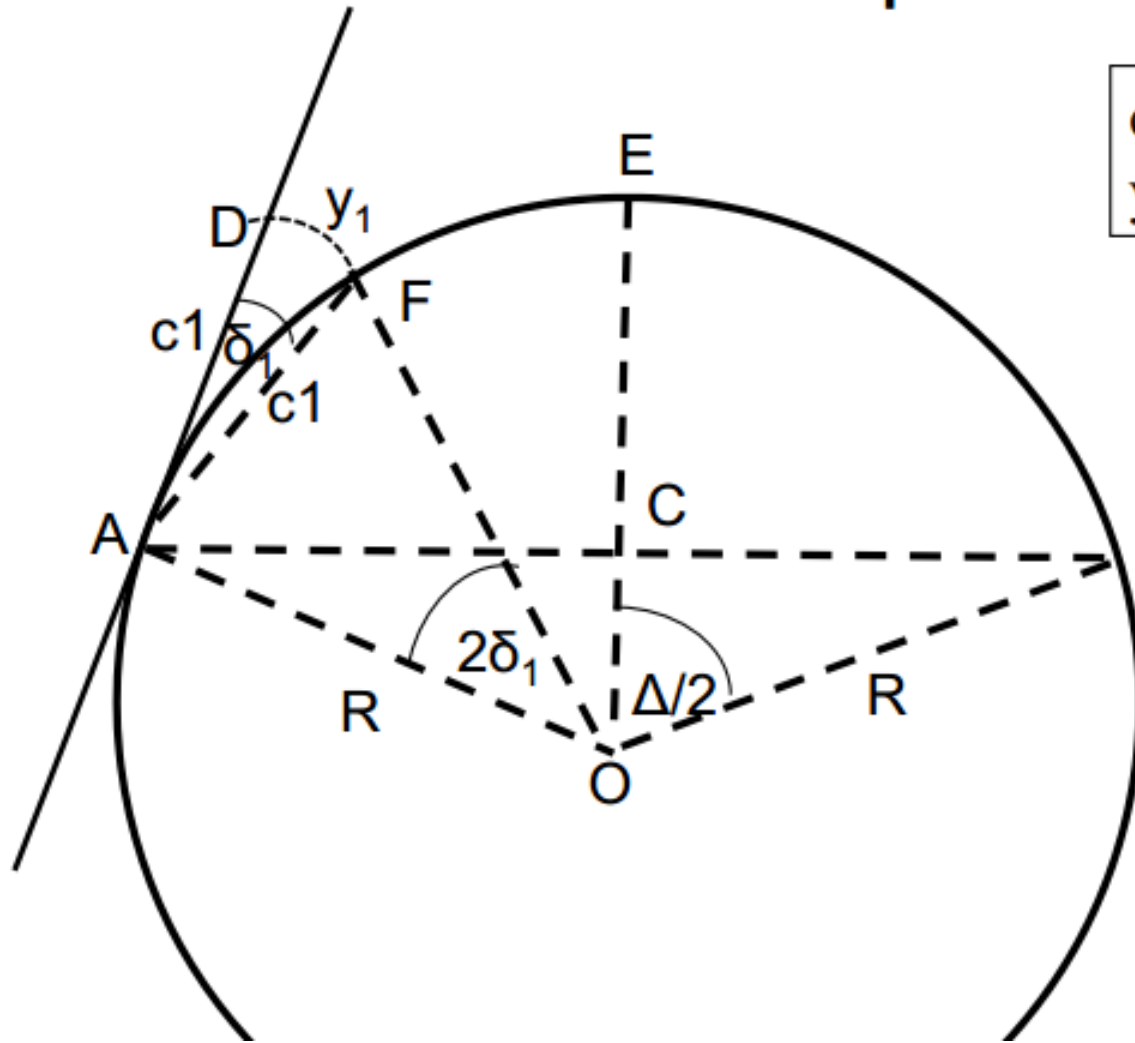
$x = \text{known}$   
 $y = ?$

$\triangle OBF \Rightarrow$

$$(R-y)^2 + x^2 = R^2$$

$$y = R - \sqrt{R^2 - x^2}$$

# offset from chords produced



$$c_1 = \text{known}$$
$$y_1 = ?$$

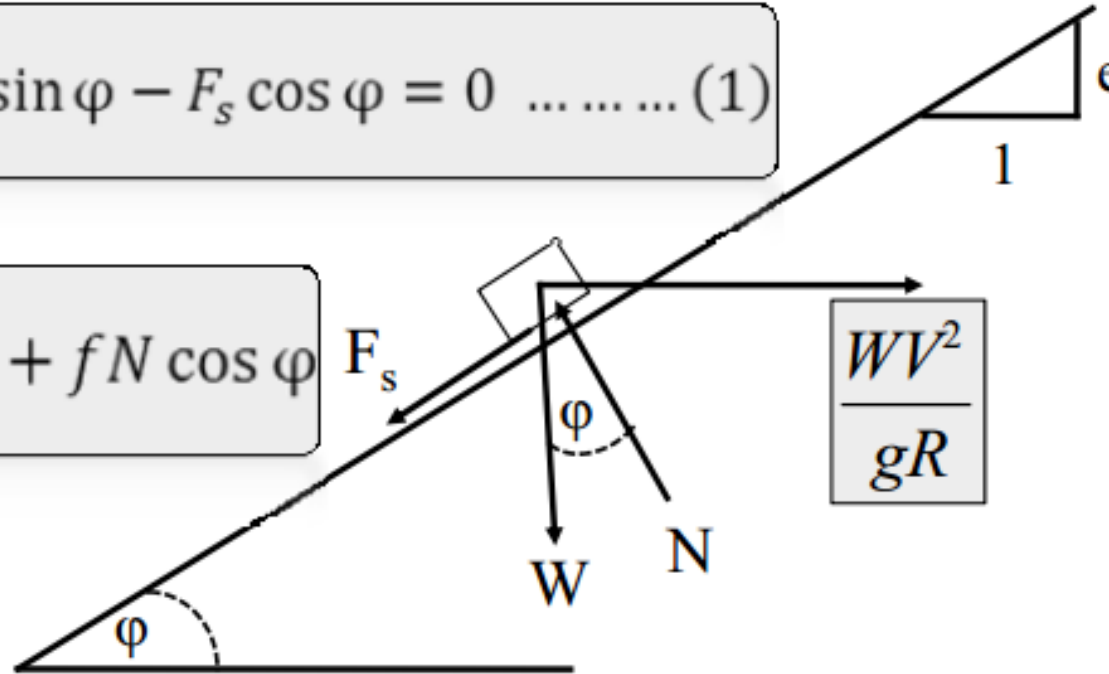
$$y_1 = c_1 \delta_1$$
$$c_1 = R(2\delta_1)$$
$$y_1 = c_1^2 / 2R$$

$$y_1 = \frac{c_1^2}{2R}$$

# Considering side friction

$$\frac{WV^2}{gR} - N \sin \varphi - F_s \cos \varphi = 0 \dots \dots \dots (1)$$

$$\frac{WV^2}{gR} = N \sin \varphi + fN \cos \varphi$$



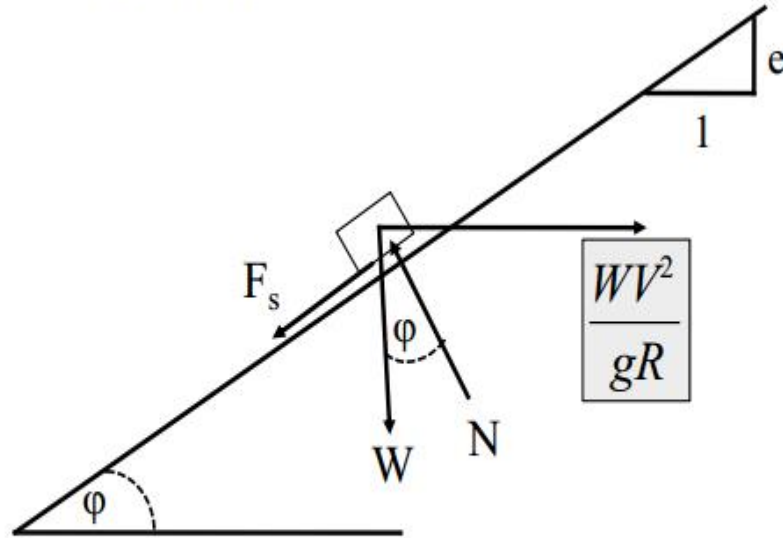
$$\frac{WV^2}{gR}$$

$$W = \frac{N}{\frac{V^2}{gR}} (\sin \varphi + f \cos \varphi)$$

$F_s = fN$ , where  $f$  is static side friction coefficient  
 $\tan \varphi = e =$  rate of super elevation

$F_s = fN$ , where  $f$  is static friction coefficient

$\tan\phi = e =$  rate of superelevation



$$-W + N \cos \phi - F_s \sin \phi = 0 \dots \dots (2)$$

$$W = N \cos \phi - fN \sin \phi = N(\cos \phi - f \sin \phi)$$

$$N(\cos \phi - f \sin \phi) = \frac{N}{\frac{V^2}{gR}} (\sin \phi + f \cos \phi)$$

$$\frac{V^2}{gR} = \frac{\sin \phi + f \cos \phi}{\cos \phi - f \sin \phi}$$

$$\frac{V^2}{gR} = \frac{\tan \phi + f}{1 - f \tan \phi}$$

$$\frac{V^2}{gR} = \frac{e + f}{1 - ef}$$

$$e + f = \frac{V^2}{gR}$$

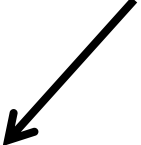
The value of the product **ef** in this equation is always small. As a result, **(1-ef)** term is normally omitted in highway and street designs, thus providing slightly more conservative values.

# Calculate the offsets (radial offset method) at 50 ft interval along tangents to locate having 3 inch cant, 0.002 friction factor and design velocity 75 mph.

$$R = \frac{V^2}{g(e + f)}$$

$$\Rightarrow R = \frac{\left(75 \times \frac{5280}{3600}\right)^2}{32 \times \left(\frac{3}{12} + 0.002\right)}$$

$$\therefore R = 1500 \text{ ft}$$

$$y = \sqrt{R^2 + x^2} - R$$


x	y
0	0
50	0.833
100	3.330
150	7.481
200	13.275



**Thank You**

**Stay Safe**

**Stay Aware**